JEE Main 2020 Paper

Date: 9th January 2020 (Shift 2)

Time: 2:30 P.M. to 5:30 P.M.

Subject: Mathematics

1. If $f(x) = \begin{vmatrix} x+a & x+2 & x+1 \\ x+b & x+3 & x+2 \\ x+c & x+4 & x+3 \end{vmatrix}$ and a-2b+c=1 then

a.
$$f(-50) = -1$$

b.
$$f(50) = 1$$

c.
$$f(50) = -501$$

d.
$$f(50) = 501$$

Answer: (a)

Given
$$f(x) = \begin{vmatrix} x+a & x+2 & x+1 \\ x+b & x+3 & x+2 \\ x+c & x+4 & x+3 \end{vmatrix}$$

$$a - 2b + c = 1$$

Applying
$$R_1 \rightarrow R_1 - 2R_2 + R_3$$

$$f(x) = \begin{vmatrix} a - 2b + c & 0 & 0 \\ x + b & x + 3 & x + 2 \\ x + c & x + 4 & x + 3 \end{vmatrix}$$

Using
$$a - 2b + c = 1$$

$$f(x) = (x+3)^2 - (x+2)(x+4)$$

$$\Rightarrow f(x) = 1$$

$$\Rightarrow f(50) = 1$$

$$\Rightarrow f(-50) = 1$$

- 2. If $f(x) = \begin{cases} x & 0 < x < \frac{1}{2} \\ \frac{1}{2} & x = \frac{1}{2} \\ 1 x & \frac{1}{2} < x < 1 \end{cases}$
 - $g(x) = \left(x \frac{1}{2}\right)^2$ then find the area bounded by f(x) and g(x) from $x = \frac{1}{2}$ to $x = \frac{\sqrt{3}}{2}$.

a.
$$\frac{\sqrt{3}}{2} - \frac{1}{3}$$

b.
$$\frac{\sqrt{3}}{4} + \frac{1}{3}$$

c.
$$2\sqrt{3}$$

d.
$$3\sqrt{3}$$

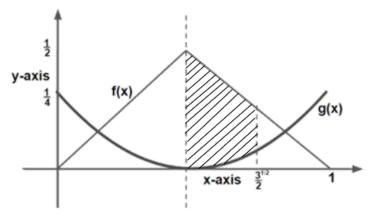
Answer: (a)

Solution:

Given
$$f(x) = \begin{cases} x & 0 < x < \frac{1}{2} \\ \frac{1}{2} & x = \frac{1}{2} \\ 1 - x & \frac{1}{2} < x < 1 \end{cases}$$

$$g(x) = (x - \frac{1}{2})^2$$

The area between f(x) and g(x) from $x = \frac{1}{2}$ to $= \frac{\sqrt{3}}{2}$:



Points of intersection of f(x) and (x):

$$1 - x = \left(x - \frac{1}{2}\right)^{2}$$

$$\Rightarrow x = \frac{\sqrt{3}}{2}, -\frac{\sqrt{3}}{2}$$
Required area
$$= \int_{\frac{1}{2}}^{\frac{\sqrt{3}}{2}} (f(x) - g(x)) dx$$

$$= \int_{\frac{1}{2}}^{\frac{\sqrt{3}}{2}} \left(1 - x - \left(x - \frac{1}{2}\right)^{2}\right) dx$$

$$= x - \frac{x^{2}}{2} - \frac{1}{3} \left(x - \frac{1}{2}\right)^{3} \Big|_{\frac{1}{2}}^{\frac{\sqrt{3}}{2}}$$

$$= \frac{\sqrt{3}}{4} - \frac{1}{3}$$

3. If $p \to (p \land \sim q)$ is false. Truth value of p and q will be

a. TF

b. FT

c. TT

d. FF

Answer: (c)

Solution:

Given $p \to (p \land \sim q)$

Truth table:

| Truth table. | | | | | | | | | |
|--------------|---|----|--------------------|--------------------------|--|--|--|--|--|
| p | q | ~q | $(p \land \sim q)$ | $p \to (p \land \sim q)$ | | | | | |
| Т | Т | F | F | F | | | | | |
| Т | F | Т | Т | Т | | | | | |
| F | Т | F | F | Т | | | | | |
| F | F | Т | F | Т | | | | | |

 $p \rightarrow (p \land \sim q)$ is false when p is true and q is true.

4. $\int \frac{d\theta}{\cos^2 \theta \ (\sec 2\theta + \tan 2\theta)} = \lambda \tan \theta + 2 \log f(x) + c \text{ then ordered pair } (\lambda, \ f(x)) \text{ is}$

a.
$$(1, 1 + \tan \theta)$$

b.
$$(1, 1 - \tan \theta)$$

c.
$$(-1, 1 + \tan \theta)$$

d.
$$(-1, 1 - \tan \theta)$$

Answer: (*c*)

Solution:

Let
$$I = \int \frac{d\theta}{\cos^2\theta(\sec 2\theta + \tan 2\theta)}$$

$$I = \int \frac{\sec^2 \theta \, d\theta}{\left(\frac{1 + \tan^2 \theta}{1 - \tan^2 \theta}\right) + \left(\frac{2 \tan \theta}{1 - \tan^2 \theta}\right)}$$

$$I = \int \frac{(1 - \tan^2 \theta)(\sec^2 \theta)d\theta}{(1 + \tan \theta)^2}$$

Let $\tan \theta = k \implies \sec^2 \theta \ d\theta = dk$

$$I = \int \frac{(1-k^2)}{(1+k)^2} dk = \int \frac{(1-k)}{(1+k)} dk$$

$$I = \left(\frac{2}{1+k} - 1\right) dk$$

$$I = 2\ln|1+k| - k + c$$

$$I = 2\ln|1 + \tan\theta| - \tan\theta + c$$

Given $I = \lambda \tan\theta + 2\log f(x) + c$

$$\therefore \lambda = -1, f(x) = |1 + tan\theta|$$

- 5. Let a_n is a positive term of GP and $\sum_{n=1}^{100} a_{2n+1} = 200$, $\sum_{n=1}^{100} a_{2n} = 100$, then the value of $\sum_{n=1}^{200} a_n$
 - a. 150

b. 225

c. 300

d. 175

Answer: (a)

Solution:

 a_n is a positive term of GP.

Let GP be a, ar, ar^2 ,

$$\sum_{n=1}^{100} a_{2n+1} = a_3 + a_5 + \dots + a_{201}$$

$$200 = ar^2 + ar^4 + \dots + ar^{201}$$

$$200 = \frac{ar^2(r^{200} - 1)}{r^2 - 1} \dots (1)$$

Also,
$$\sum_{n=1}^{100} a_{2n} = 100$$

$$100 = a_2 + a_4 + \dots + a_{200}$$

$$100 = ar + ar^3 + \dots + ar^{199}$$

$$100 = \frac{ar(r^{200} - 1)}{r^2 - 1} \dots (2)$$

From (1) and (2), r = 2

And
$$\sum_{n=1}^{100} a_{2n+1} + \sum_{n=1}^{100} a_{2n} = 300$$

$$\Rightarrow a_2 + a_3 + a_4 \dots + a_{200} + a_{201} = 300$$

$$\Rightarrow ar + ar^2 + ar^3 + \dots + ar^{200} = 300$$

$$\Rightarrow r(a+ar+ar^2+\ldots\ldots+ar^{199})=300$$

$$\Rightarrow 2(a_1 + a_2 + a_3 + \dots + a_{200}) = 300$$
$$\sum_{n=1}^{200} a_n = 150$$

- 6. z is a complex number such that |Re(z)| + |Im(z)| = 4, then |z| cannot be equal to
 - a. $\sqrt{8}$

b. $\sqrt{7}$

c. $\sqrt{\frac{17}{2}}$

d. $\sqrt{10}$

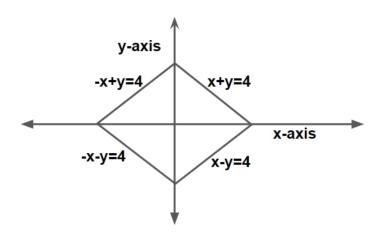
Answer: (b)

Solution:

$$|\operatorname{Re}(z)| + |\operatorname{Im}(z)| = 4$$

Let
$$z = x + iy$$

$$\Rightarrow |x| + |y| = 4$$



 \therefore z lies on the rhombus.

Maximum value of |z| = 4 when z = 4, -4, 4i, -4i

Minimum value of $|z| = 2\sqrt{2}$ when $z = 2 \pm 2i$, $\pm 2 + 2i$

$$|z| \in [2\sqrt{2}, 4]$$

$$|z| \in [\sqrt{8}, \sqrt{16}]$$

$$|z| \neq \sqrt{7}$$

7.
$$f(x): [0,5] \to R, F(x) = \int_0^x x^2 g(x) dx$$
, $f(1) = 3$, $g(x) = \int_1^x f(t) dt$ then correct choice is

- a. F(x) has no critical point
- b. F(x) has local minimum at x = 1
- c. F(x) has local maximum at x = 1
- d. F(x) has point of inflection at x = 1

Answer: (b)

$$F(x) = x^2 g(x)$$

Put
$$x = 1$$

$$\Rightarrow F(1) = g(1) = 0$$
 ... (1)

 $\operatorname{Now} F''(x) = 2xg(x) + g'(x)x^2$

$$F''(1) = 2g(1) + g'(1)$$
 {: $g'(x) = f(x)$ }

$$F''(1) = f(1) = 3$$
 ...(2)

From (1) and (2), F(x) has local minimum at x = 1

- 8. Let $x=2\sin\theta-\sin2\theta$ and $y=2\cos\theta-\cos2\theta$, then the value of $\frac{d^2y}{dx^2}$ at $\theta=\pi$ is
 - a. $\frac{3}{8}$

b. $\frac{5}{8}$

c. $\frac{7}{8}$

d. $\frac{3}{2}$

Answer: (a)

$$\frac{dx}{d\theta} = 2\cos\theta - 2\cos 2\theta$$

$$\frac{dy}{d\theta} = -2\sin\theta + 2\sin 2\theta$$

$$\frac{dy}{dx} = \frac{2\cos\frac{3\theta}{2}\sin\frac{\theta}{2}}{2\sin\frac{3\theta}{2}\sin\frac{\theta}{2}}$$

$$\frac{dy}{dx} = \cot \frac{3\theta}{2}$$

$$\frac{d^2y}{dx^2} = -\frac{3}{2} \csc^2 \frac{3\theta}{2} \frac{d\theta}{dx}$$

$$\frac{d^2y}{dx^2} = \left(-\frac{3}{2}\cos ec^2\frac{3\theta}{2}\right)\frac{1}{(2\cos\theta - 2\cos 2\theta)}$$

$$\left. \frac{d^2 y}{dx^2} \right|_{\theta = \pi} = \frac{3}{8}$$

- 9. If f(x) and g(x) are continuous functions, $f \circ g$ is identity function, g'(b) = 5 and g(b) = a, then f'(a) is
 - a. $\frac{3}{5}$

b. 5

c. $\frac{2}{5}$

d. $\frac{1}{5}$

Answer: (d)

Solution:

$$f(g(x)) = x$$

$$f'(g(x))g'(x) = 1$$

Put
$$x = b$$

$$f'(g(b))g'(b) = 1$$

$$f'(a) \times 5 = 1$$

$$f'(a) = \frac{1}{5}$$

10. Let x + 6y = 8 is tangent to standard ellipse where minor axis is $\frac{4}{\sqrt{3}}$, then eccentricity of ellipse is

a.
$$\frac{1}{4}\sqrt{\frac{11}{12}}$$

b.
$$\frac{1}{4}\sqrt{\frac{11}{3}}$$

c.
$$\sqrt{\frac{5}{6}}$$

d.
$$\sqrt{\frac{11}{12}}$$

Answer: (d)

If
$$2b = \frac{4}{\sqrt{3}}$$

$$b = \frac{2}{\sqrt{3}}$$

Comparing
$$y = -\frac{x}{6} + \frac{8}{6}$$
 with $y = mx \pm \sqrt{a^2m^2 + b^2}$

$$m = -\frac{1}{6}$$
 and $a^2m^2 + b^2 = \frac{16}{9}$

$$\frac{a^2}{36} + \frac{4}{3} = \frac{16}{9}$$

$$\Rightarrow \frac{a^2}{36} = \frac{16}{9} - \frac{4}{3}$$

$$\Rightarrow a^2 = 16$$

$$e = \sqrt{1 - \frac{b^2}{a^2}}$$

$$\Rightarrow e = \sqrt{\frac{11}{12}}$$

11. If one end of focal chord of parabola $y^2 = 8x$ is $\left(\frac{1}{2}, -2\right)$, then the equation of tangent at the other end of this focal chord is

a.
$$x + 2y + 8 = 0$$

b.
$$x - 2y = 8$$

c.
$$x - 2y + 8 = 0$$

d.
$$x + 2y = 8$$

Answer: (c)

Solution:

Let PQ be the focal chord of the parabola $y^2 = 8x$

$$\Rightarrow P(t_1) = (2t_1^2, 4t_1) \& Q(t_2) = (2t_2^2, 4t_2)$$

$$\Rightarrow t_1 t_2 = -1$$

 $\because \left(\frac{1}{2}, -2\right)$ is one of the ends of the focal chord of the parabola

Let
$$\left(\frac{1}{2}, -2\right) = (2t_2^2, 4t_2)$$

$$\Rightarrow t_2 = -\frac{1}{2}$$

- \Rightarrow Other end of focal chord will have parameter $t_1=2$
- \Rightarrow The co-ordinate of the other end of the focal chord will be (8,8)
- ∴ The equation of the tangent will be given as $\rightarrow 8y = 4(x + 8)$

$$\Rightarrow 2y - x = 8$$

- 12. If 7x + 6y 2z = 0, 3x + 4y + 2z = 0 & x 2y 6z = 0, then the system of equations has
 - a. No solution
 - b. Infinite non-trivial solution for (x = 2z)
 - c. Infinite non-trivial solution for (y = 2z)
 - d. Only trivial solution

Answer: (b)

Solution:

$$7x + 6y - 2z = 0$$

$$3x + 4y + 2z = 0$$

$$x - 2y - 6z = 0$$

As the system of equations are Homogeneous \Rightarrow the system is consistent.

$$\Rightarrow \begin{vmatrix} 7 & 6 & -2 \\ 3 & 4 & 2 \\ 1 & -2 & -6 \end{vmatrix} = 0$$

⇒ Infinite solutions exist (both trivial and non-trivial solutions)

When y = 2z

Let's take y = 2, z = 1

When (x, 2, 1) is substituted in the system of equations

$$\Rightarrow$$
 7 x + 10 = 0

$$3x + 10 = 0$$

x - 10 = 0 (which is not possible)

 $\therefore y = 2z \Rightarrow$ Infinite non-trivial solutions does not exist.

For x = 2z, lets take x = 2, z = 1, y = y

Substitute (2, y, 1) in system of equations

$$\Rightarrow$$
 $y = -2$

 \therefore For each pair of (x, z), we get a value of y.

Therefore, for x = 2z infinite non-trivial solution exists.

- 13. If both the roots of the equation $ax^2 2bx + 5 = 0$ are α and of the equation $x^2 2bx 10 = 0$ are α and β . Then the value of $\alpha^2 + \beta^2$
 - a. 15

b. 20

c. 25

d. 30

Answer: (c)

 $ax^2 - 2bx + 5 = 0$ has both roots as α

$$\Rightarrow 2\alpha = \frac{2b}{a} \Rightarrow \alpha = \frac{b}{a}$$

And
$$\alpha^2 = \frac{5}{a}$$

$$\Rightarrow b^2 = 5a(a \neq 0) \qquad \dots (1)$$

$$\Rightarrow \alpha + \beta = 2b \& \alpha\beta = -10$$

$$\alpha = \frac{b}{a}$$
 is also a root of $x^2 - 2bx - 10 = 0$

$$\Rightarrow b^2 - 2ab^2 - 10a^2 = 0$$

$$b^2 = 5a \Rightarrow 5a - 10a^2 - 10a^2 = 0$$

$$\Rightarrow a = \frac{1}{4} \Rightarrow b^2 = \frac{5}{4}$$

$$\Rightarrow \alpha^2 = 20, \beta^2 = 5$$

$$\Rightarrow \alpha^2 + \beta^2 = 25$$

14. If $A = \{x: |x| < 2 \text{ and } B = \{x: |x-2| \ge 3\}$ then

a.
$$A \cap B = [-2, -1]$$

c.
$$A - B = [-1,2)$$

b.
$$B - A = \mathbf{R} - (-2.5)$$

d.
$$A \cup B = \mathbf{R} - (2,5)$$

 $\textbf{Answer:}\ (b)$

$$A = \{x : x \in (-2,2)\}$$

$$B = \{x : x \in (-\infty, -1] \cup [5, \infty)\}$$

$$A \cap B = \{x : x \in (-2, -1]\}$$

$$B - A = \{x : x \in (-\infty, -2] \cup [5, \infty)\}$$

$$A - B = \{x : x \in (-1,2)\}$$

$$A \cup B = \{x : x \in (-\infty, 2) \cup [5, \infty)\}$$

15. The value of $P(x_i > 2)$ for the given probability distribution is

| x_i | 1 | 2 | 3 | 4 | 5 |
|-------|-------|----|---|----|----------|
| P_i | k^2 | 2k | k | 2k | $5k^{2}$ |

a. $\frac{1}{36}$

b. $\frac{23}{36}$

c. $\frac{1}{6}$

d. $\frac{7}{12}$

Answer: (b)

Solution:

We know that $\sum_{x_i=1}^5 P_i = 1$

$$\Rightarrow k^2 + 2k + k + 2k + 5k^2 = 1$$

$$\Rightarrow k = -1, \frac{1}{6} : k = \frac{1}{6}$$

$$P(x_i > 2) = P(x_i = 3) + P(x_i = 4) + P(x_i = 5)$$
$$= k + 2k + 5k^2 = \frac{23}{36}$$

- 16. Let the distance between the plane passing through lines $\frac{x+1}{2} = \frac{y-3}{3} = \frac{z+1}{8}$ and $\frac{x+3}{2} = \frac{y+2}{1} = \frac{z-1}{\lambda}$ and the plane 23x 10y 2z + 48 = 0 is $\frac{k}{\sqrt{633}}$, then the value of k is
 - a. 4

h. 3

c. 2

d. 1

Answer: (b)

Solution:

We find the point of intersection of the two lines, and the distance of given plane from the two lines is the distance of plane from the point of intersection.

$$\therefore (2p-1, 2p+3, 8p-1) = (2q-3, q-2, \lambda q+1)$$

$$p = -2$$
 and $q = -1$

$$\lambda = 18$$

Point of intersection is (-5, -3, -17)

$$\therefore \frac{k}{\sqrt{633}} = \left| \frac{-115 + 30 + 34 + 48}{\sqrt{633}} \right| \Rightarrow k = 3$$

17. Let
$$x = \sum_{n=0}^{\infty} (-1)^n (\tan \theta)^{2n}$$
 and $y = \sum_{n=0}^{\infty} (\cos \theta)^{2n}$, where $\theta \in (0, \frac{\pi}{4})$, then

a.
$$y(x-1) = 1$$

b.
$$y(1-x) = 1$$

c.
$$x(y+1) = 1$$

d. y(1+x) = 1

Answer: (b)

Solution:

$$y = 1 + \cos^2 \theta + \cos^4 \theta + \cdots$$

$$\Rightarrow y = \frac{1}{1 - \cos^2 \theta} \Rightarrow \frac{1}{y} = \sin^2 \theta$$

$$x = 1 - \tan^2 \theta + \tan^4 \theta - \cdots$$

$$\Rightarrow x = \frac{1}{1 - (-\tan^2 \theta)} = \cos^2 \theta$$

$$x = 1 - \tan^2 \theta + \tan^4 \theta - \cdots$$

$$\Rightarrow x = \frac{1}{1 - (-\tan^2 \theta)} = \cos^2 \theta$$

$$\therefore x + \frac{1}{y} = 1 \Rightarrow y(1 - x) = 1$$

18. If $\lim_{x\to 0} x \left[\frac{4}{x}\right] = A$, then the value of x at which $f(x) = [x^2] \sin \pi x$ is discontinuous at (where [.] denotes greatest integer function)

a.
$$\sqrt{A+5}$$

b.
$$\sqrt{A+1}$$

c.
$$\sqrt{A + 21}$$

d.
$$\sqrt{A}$$

Answer: (b)

Solution:

$$f(x) = [x^2] \sin \pi x$$

It is continuous $\forall x \in \mathbf{Z}$ as $\sin \pi x \to 0$ as $x \to \mathbf{Z}$.

f(x) is discontinuous at points where $[x^2]$ is discontinuous i.e. $x^2 \in \mathbf{Z}$ with an exception that f(x) is continuous as x is an integer.

 \therefore Points of discontinuity for f(x) would be at

$$x = \pm \sqrt{2}, \pm \sqrt{3}, \pm \sqrt{5}, \dots$$

Also, it is given that $\lim_{x\to 0} x \left[\frac{4}{x}\right] = A$ (indeterminate form $(0 \times \infty)$)

$$\Rightarrow \lim_{x \to 0} x \left(\frac{4}{x} - \left\{ \frac{4}{x} \right\} \right) = A$$

$$\Rightarrow 4 - \lim_{x \to 0} \left\{ \frac{4}{x} \right\} = A$$

$$\Rightarrow A = 4$$

$$\sqrt{A+5}=3$$

$$\sqrt{A+1} = \sqrt{5}$$

$$\sqrt{A+21}=5$$

$$\sqrt{A} = 2$$

- \therefore Points of discontinuity for f(x) is $x = \sqrt{5}$
- 19. Circles $(x 0)^2 + (y 4)^2 = k$ and $(x 3)^2 + (y 0)^2 = 1^2$ touch each other. The maximum value of k is _____.

Answer: (36)

Solution:

Two circles touch each other if $C_1C_2 = |r_1 \pm r_2|$

$$\sqrt{k} + 1 = 5 \text{ or } |\sqrt{k} - 1| = 5$$

$$\Rightarrow k = 16 \text{ or } 36$$

Maximum value of k is 36

20. If
$${}^{25}C_0 + 5{}^{25}C_1 + 9{}^{25}C_2 + \dots + 101{}^{25}C_{25} = 2{}^{25}k$$
, then the value of k is _____.

Answer: (51)

Solution:

$$S = {}^{25}C_0 + 5{}^{25}C_1 + 9{}^{25}C_2 + \dots + 97{}^{25}C_{24} + 101{}^{25}C_{25} = 2{}^{25}k \tag{1}$$

Reverse and apply property ${}^{n}C_{r} = {}^{n}C_{n-r}$ in all coefficients

$$S = 101^{25}C_0 + 97^{25}C_1 + \dots + 5^{25}C_{24} + {}^{25}C_{25}$$
 (2)

Adding (1) and (2), we get

$$2S = 102[^{25}C_0 + ^{25}C_1 + \dots + ^{25}C_{25}]$$

$$S = 51 \times 2^{25}$$

$$\Rightarrow k = 51$$

21. Number of common terms in both the sequences 3, 7, 11, ... 407 and 2, 9, 16, ... 905 is ______.

Answer: (14)

Solution:

First common term is 23

Common difference = LCM(7, 4) = 28

$$23 + (n-1)28 \le 407$$

$$n - 1 \le 13.71$$

n = 14

22. Let $|\vec{a}| = \sqrt{3}$, $|\vec{b}| = 5$, \vec{b} . $\vec{c} = 10$ and angle between \vec{b} and \vec{c} is equal to $\frac{\pi}{3}$. If \vec{a} is perpendicular to $\vec{b} \times \vec{c}$, then the value of $|\vec{a} \times (\vec{b} \times \vec{c})|$ is

Answer: (30)

Solution:

$$|\vec{a} \times (\vec{b} \times \vec{c})| = |\vec{a}| |\vec{b} \times \vec{c}| \sin \theta$$
 where θ is the angle between \vec{a} and $\vec{b} \times \vec{c}$

$$\theta = \frac{\pi}{2}$$
 given

$$\Rightarrow |\vec{a} \times (\vec{b} \times \vec{c})| = \sqrt{3} |\vec{b} \times \vec{c}| = \sqrt{3} |\vec{b}| |\vec{c}| \sin \frac{\pi}{3}$$

$$\Rightarrow \left| \vec{a} \times \left(\vec{b} \times \vec{c} \right) \right| = \sqrt{3} \times 5 \times |\vec{c}| \times \frac{\sqrt{3}}{2}$$

$$\Rightarrow \left| \vec{a} \times \left(\vec{b} \times \vec{c} \right) \right| = \frac{15}{2} |\vec{c}|$$

Now,
$$|\vec{b}||\vec{c}|\cos\theta = 10$$

$$5|\vec{c}|^{\frac{1}{2}}=10$$

$$|\vec{c}| = 4$$

23. If minimum value of term free from x for $\left(\frac{x}{\sin\theta} + \frac{1}{x\cos\theta}\right)^{16}$ is L_1 in $\theta \in \left[\frac{\pi}{8}, \frac{\pi}{4}\right]$ and L_2 in $\theta \in \left[\frac{\pi}{16}, \frac{\pi}{8}\right]$, the value of $\frac{L_2}{L_1}$ is

Answer: (16)

Solution:

$$T_{r+1} = {}^{16}C_r \left(\frac{x}{\sin \theta}\right)^{16-r} \left(\frac{1}{x \cos \theta}\right)^r$$

For term independent of x,

$$16 - 2r = 0 \Rightarrow r = 8$$

$$T_9 = {}^{16}C_8 \left(\frac{1}{\sin\theta\cos\theta}\right)^8 = {}^{16}C_8 2^8 \left(\frac{1}{\sin2\theta}\right)^8$$

$$L_1 = {}^{16}C_8 2^8$$
 at $\theta = \frac{\pi}{4}$

$$L_2 = {}^{16}C_8 \frac{2^8}{\left(\frac{1}{\sqrt{2}}\right)^8} = {}^{16}C_8 2^{12}$$
 at $\theta = \frac{\pi}{8}$

$$\frac{L_2}{L_1} = 16$$